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# **Particle Image Velocimetry**

## **A Practical Guide**

Second Edition

With 288 Figures and 42 Tables

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